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# **Ghost tomography**

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The quest for imaging protocols with ever-reduced dose is one of the most powerful motivators driving the currently 11 12 exploding field of ghost imaging (GI). Ghost tomography (GT) using single-pixel detection extends the burgeoning 13 field of GI to 3D, with the use of penetrating radiation. For hard x rays, GT has the potential to relax the constraints that dose rate and detector performance impose on image quality and resolution. In this work, spatially random x-ray 14 intensity patterns illuminate a specimen from various view-angles; in each case, the total transmitted intensity is re-15 corded by a single-pixel (or bucket) detector. These readings, combined with knowledge of the corresponding 2D 16 17 illuminating patterns and specimen orientations, are sufficient for 3D specimen reconstruction. The experimental 18 demonstration of GT is presented here using synchrotron hard x rays. This result significantly expands the scope of GI to encompass volumetric imaging (i.e., tomography), of optically opaque objects using penetrating 19 20 radiation. © 2018 Optical Society of America under the terms of the OSA Open Access Publishing Agreement

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## 21 1. INTRODUCTION

22 Ghost imaging (GI) first emerged in the domain of visible-light optics [1]. The term arose from Einstein's description of quantum 23 entanglement as "spooky action at a distance," since initial real-24 izations of the method utilized pairs of entangled photons. 25 26 Classical implementations of GI have since been developed using pairs of correlated, coherent wave fields [2]. Very recently, GI 27 been achieved with atoms [3], electrons [4], and x rays [5-10]. 28 However, to date, none of the reported studies utilizing penetrat-29 30 ing radiation have attempted to map the interior structure of a genuinely three-dimensional (3D) sample. GI clearly has the po-31 32 tential to achieve such tomographic reconstruction, constituting a natural extension of previously reported lower-dimensional ghost 33 images. Here we report on the realization of ghost tomography 34 (GT) using hard x rays, whose penetrating power for optically 35 opaque objects significantly extends both the applicability and 36 utility of the technique. 37

38 Synthesizing images via the superposition of linearly independent intensity maps, random or otherwise, is the essence of GI 39 [11–14]. These maps, when random, may be generated through 40 quantum processes such as shot noise or through classical means 41 42 such as spatially random masks. Nonrandom intensity maps may be generated using suitable deterministic masks. We restrict con-43 sideration to random illuminating intensity maps for the remain-44 der of this paper on account of their ease of construction for x-ray 45 fields. A key feature of GI is that the ensemble of superposed 46

linearly independent illuminating intensity maps is formed by photons (or other imaging quanta) that never pass through the sample. A weak copy of the illuminating field, which may be obtained, e.g., using a beam splitter, does pass through the object but only the total number of transmitted quanta is measured by a single-pixel detector in a so-called "bucket signal."

3D GT of optically opaque objects has not been demonstrated in the literature; however, similar concepts have been presented. Direct (as opposed to computed) GT of optically transparent objects has been reported using optical coherence imaging [15]. Ghost topography (or 3D surface imaging by GI) has been developed in a remote sensing context using time-of-flight with a single-pixel camera [16]. 2D GT with terahertz radiation has been presented by Mohr *et al.* [17].

Since no imaging quanta that pass through the sample are ever registered by a position-sensitive detector, GIresolution is independent of the bucket detector. This is an important distinction between GT and computed tomography (CT): in CT, 3D volume resolution is limited by the pixel size of the detector. In CT, the pixel size of the detector and geometric magnification of the imaging system immediately suggest an appropriate discretization (i.e., voxel size) for the 3D volume; in GT, the correct 3D discretization must be found based on analysis of the ensemble of illuminating fields.

In two-dimensional (2D) GI applications, the parallelized intensity–intensity cross-correlation between the bucket and any one pixel of the random reference maps is used to compute 47

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the ghost image [11,12]. In what follows, we show that simply combining this method with tomography can be insufficient for 3D imaging, and we present new reconstruction schemes that give superior results. Our experimental proof-of-concept for GT significantly expands the scope of GI, empowering it to realize genuinely 3D reconstructions.



F1:1 Fig. 1. Experimental setup for x-ray GT. Synchrotron x rays from an F1:2 undulator are passed through a spatially random mask (not shown). The F1:3 resulting random 2D speckled beam is split into two copies by a crystal F1:4 beam splitter working in a Laue diffraction condition. The diffracted F1:5 beam, much weaker in intensity than the direct beam, is passed through F1:6 the sample before being registered at the position-insensitive bucket de-F1:7 tector. The direct beam, consisting of photons that never pass through F1:8 the object, is measured over the position-sensitive detector. An ensemble F1:9 of spatially random illuminating patterns is created by transversely displacing the mask. Note that only the spatially integrated signal (termed F1:10 F1:11 the "bucket signal") for each bucket-beam measurement is utilized in the F1:12 x-ray GT. The process is repeated for a variety of angular orientations  $\theta$  of F1:13 the sample.

#### 2. METHOD

A schematic of our experimental setup for x-ray GT is shown in Fig. 1. Illumination of a spatially random 1-mm-thick Ni foam with normally incident 26 keV hard x rays from a synchrotron created spatially random intensity illumination patterns, such as that shown in Fig. 2A. An ensemble of such speckle patterns was obtained via transverse displacement of the foam over a 2D square grid with a step size of 400  $\mu$ m. This transverse step size was chosen to be considerably larger than the width of the illuminating speckle intensity autocovariance (Fig. 2C), to reduce the 1 degree of correlation between illuminating speckle images. The sample for our proof-of-concept x-ray GT experiment was an Al cylinder with diameter 5.60 mm, into which was drilled two cylindrical holes with respective diameters of 1.98 and 1.50 mm (Fig. 2B). This sample was secured to a rotation stage and illuminated with attenuated copies of the spatially random intensity maps, obtained by using a 220 Laue x-ray reflection from a (001) Si wafer beam splitter.

Approximately 2000 random-illumination intensity maps were used, forming a linearly independent mathematical basis [13] for the 2D ghost projection images. Noise-free simulations, assuming a similar experimental setup with 64<sup>2</sup> pixel illumination patterns, were conducted in Kingston *et al.* [18]. These showed image quality (using conventional GI) degraded as the number of illumination patterns was reduced, and that 1000 patterns per view-angle approached the lower limit of object resolvability. Regularization techniques, such as compressed sensing, were shown to produce significant image quality improvements; however, given that the data measured here would contain noise and other artifacts, we opted for 2000 measurements per view-angle.

GI spatial resolution [19] cannot be determined based on pixel110size, so we have therefore used Fourier ring correlation (FRC)-111applied to the ensemble of illuminating speckle fields-to estimate112the resolution of our imaging system as approximately 100 μm113(Supplement 1). FRC yields a best-case limit estimate for 2D spa-114tial resolution. This is quite distinct from the point spread func-115tion (PSF) of the 2D imaging system (Fig. 2C) that is calculated as116



F2:1 Fig. 2. (A) Example of spatially random x-ray intensity illumination pattern; LHS, as measured; RHS, blurred to match motion artifacts in bucket F2:2 image. Yellow box [coinciding with blue box in Fig. 2(D)] indicates region used for GI/GT. (B) Schematic of Al phantom sample; (C) PSF found as the F2:3 normalized autocovariance of the set of illuminating spatially random fields; LHS, as measured; RHS, blurred to match motion artifacts in bucket image. F2:4 Zoom ×4 presented in top-right corner. (D) Example bucket image with the blue box indicating the region over which the signal was accumulated to give F2:5 the single-pixel bucket signal. (E) FRC results from registered image subsets, used to determine 3D GI resolution (determined as the reciprocal distance at F2:6 which correlation drops below 1 bit). The relevant (spck/bckt) resolution result of 100 µm, was used to select the 3D discretization for the tomographic reconstructions in Fig. 3. Image pairs include: spck/spck, –speckle images compared at  $\theta = 0^{\circ}$  and  $\theta = 68.750^{\circ}$ ; spck/blur, –speckle image at  $\theta = 0^{\circ}$ F2:7 F2:8 compared to blurred speckle image at  $\theta = 68.750^\circ$ ; bckt/bckt, bucket images compared at  $\theta = 0^\circ$  and  $\theta = 68.750^\circ$ ; spck/bckt, speckle image at  $\theta = 0^\circ$ F2:9 compared to bucket image at  $\theta = 0^{\circ}$ .

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the normalized autocovariance of the set of illuminating spatially 117 random intensity fields [9,19]; this PSF estimates the resolution 118 119 of conventional GI by cross-correlation [11,12]. In either case, the 120 theoretically achievable resolution is limited below by twice the 121 pixel size of the detector used to measure the illumination pat-122 terns. See Section 2A in Supplement 1 for further detail. These 123 estimates of resolution allow us to select an appropriate discreti-124 zation for our 3D reconstructed image.

For tomographic imaging, we repeated the 2000 random-125 illumination intensity maps for each of N = 14 projection 126 angles. Due to some instability of the beam-line vacuum, the 127 128 x-ray beam dropped out at random time intervals during data ac-129 quisition. Unlike conventional CT, GI is insensitive to such 130 random signal dropouts because it utilizes intensity-intensity correlations. Further, the object rotation angles were chosen using a 131 132 quasi-random (or low-discrepancy) additive recurrence sequence of angles,  $\theta$ , with step size equal to 133

 $\Delta \theta = \pi(\phi - 1) \tag{1}$ 

134 rad, where

$$\phi = \left(1 + \sqrt{5}\right)/2\tag{2}$$

is the golden ratio. This equates to  $\Delta \theta = 111.25^{\circ}$  and can be achieved equivalently with an angular step size for the object rotations of  $180^{\circ} - 111.25^{\circ} = 68.75^{\circ}$ . Quasi-random sequences appear to be random locally but are highly ordered globally. Hence, at any time the experiment is ceased, the angle set acquired will be an approximately uniform sampling of  $[0, \pi)$  rad.

141 2 Each detected image was registered via an indirect detector, consisting of a scintillator screen, lens system and a 2560 × 142 2160 pixel pco.edge 5.5 (PCO AG, Germany) sCMOS-based 143 camera with pixel pitch of 6.5 µm, and binned down to the res-144 olution that was determined via FRC. Each object-free 2D refer-145 146 ence-illumination beam was paired with a bucket-beam image containing the object (e.g., blue box in Fig. 2D corresponding 147 148 to yellow box in Fig. 2A). The total signal in the blue-box region was summed to give the bucket signal  $B_{i,\theta}$  corresponding to the 149 *i*th realization of the spatially random illuminating pattern, at 150 sample rotation angle  $\theta$ . The spatially random intensity pattern 151  $I_i(x, y)$  illuminating this same region corresponds to the spatially 152 resolved intensity map of the beam that did not pass through 153 the object, where (x, y) are Cartesian coordinates in the detector 154 155 plane.

## 156 3. ANALYSIS AND RESULTS

157 In 2D GI, the cross-correlation GI formula [11,12] may be used 158 to estimate the 2D intensity transmission function  $T(x, y; \theta)$  for a 159 given fixed object rotation  $\theta$  as the ensemble average (intensity– 160 intensity correlation):

$$T(x, y; \theta) = \frac{1}{M(\theta)} \sum_{j=1}^{M(\theta)} I_j(x, y) (B_{j,\theta} - B_{av,\theta}).$$
(3)

161 Here,  $B_{av,\theta}$  is the average bucket signal for a given  $\theta$ , and  $M(\theta)$  is 162 the number of bucket measurements taken at each orientation. 163 This ensemble average constitutes the superposition of linearly 164 independent spatially random intensity maps  $I_j(x, y)$  referred 165 to above. Subsequent reconstruction of the 3D attenuation func-166 tion using conventional tomography algorithms showed that 167 the cross-correlation GI formula is inadequate for 3D imaging (see Figs. S8a and S8d of Supplement 1 and accompanying text168in Section S4B). A posteriori information of the sample must be169leveraged to produce a meaningful GT reconstruction. To achieve170this, we employed iterative cross-correlation via the Landweber171algorithm coupled with smoothness priors [18]. The relaxation172parameter used was173

$$\gamma = 0.01/(J_{\theta}\sigma^2), \qquad (4)$$

where  $J_{\theta}$  is the number of measurement pairs at angle  $\theta$ , and  $\sigma^2$  is the variance of the spatially random speckle patterns. Such a 2D 175 reconstruction was performed for each of the 14 pseudo-random 176 projection angles  $\theta$ . Applying conventional tomographic 177 reconstruction techniques to the resulting projection images produced a reasonable but very noisy tomogram (see Figs. S8b–c and 179 S8e–f in Supplement 1 and accompanying text in Section S4B). 180

In the above two-step reconstruction scheme (ghost 181 reconstruction followed by tomography), each projection image 182 is reconstructed separately from the others. This is not the optimal 183 approach, as projections at different angles are obviously related. 184 A better result can be achieved by direct reconstruction, where 185 one recovers the 3D volume directly from the bucket signals, thus 186 using all measured information simultaneously; the intermediate 187 step of recovering the 2D x-ray ghost projection images can be 188 removed. A gradient descent (or the Landweber) algorithm for 189 direct iterative tomographic reconstruction from bucket signals 190 has very recently been developed in Section V of the simula-191 tion-based study of Kingston et al. [18]. A smoothness prior 192 and enforced positivity in attenuation coefficient were included 193 here to improve the result. Vertical and horizontal slices through 194 the resulting x-ray GT reconstructions are shown in Figs. 3A and 195 3B, respectively. These may be compared to the conventional CT 196 reconstructions obtained in the same set of experiments, as given 197 in Figs. 3C and 3D. A semitransparent rendering of the 3D re-198 constructed ghost tomogram is given in Fig. 3E, with horizontal 199 and vertical cutaway 3D renderings in Figs. 3F and 3G, respec-200 tively. The nontrivial preprocessing steps required to achieve the 201



Fig. 3. Horizontal (A) and vertical (B) 2D slices through the 3D x-ray F3:1 GT reconstructed volume with a voxel pitch of 48 µm. The correspond-F3:2 ing horizontal (C) and vertical (D) 2D slices through the conventional F3:3 3D tomography reconstructed volume obtained from the same set of ex-F3:4 periments. (E) A semitransparent rendering of the 3D GT reconstructed F3:5 object indicating the location of the slices (A) and (B). Horizontal (F) and F3:6 vertical (G) cutaway images of the rendered ghost-tomogram volume F3:7 showing the position of slices (A) and (B), respectively. Note that the F3:8 blue lines in (A) and (C) indicate the position of the orthogonal slices F3:9 (B) and (D); likewise, the red lines in (B) and (D) indicate the location F3:10 of perpendicular slices (A) and (C). F3:11

results in Fig. 3 are detailed in Supplement 1. This supplement 202 also gives further GI tomographic slices in Fig. S9. The recon-203 structed sample densities, as obtained from the x-ray ghost tomo-204 205 **3** grams, are quantitative. Using the XCOM (NIST) database [20], 206 the attenuation per unit density of Al at 26 keV is  $1.65 \text{ cm}^2/\text{g}$ . The density of Al is 2.70 g/cm<sup>3</sup>, giving an expected linear attenu-207 ation coefficient of 4.455 cm<sup>-1</sup>. From the reconstructed x-ray 208 209 ghost tomogram with 52 µm pixel dimension (i.e., binned ×8) the mean attenuation of the Al is measured as 4.80 cm<sup>-1</sup> and cor-210 211 responds to the attenuation of Al at 25.3 keV. This increase in 212 attenuation is most likely due to inclusions of higher-Z metals to 213 form the Al alloy, together with the difference in spectrum 214 between the direct and diffracted beams.

### 215 4. DISCUSSION

216 The ability to achieve quantitative 3D imaging, in a GI geometry where none of the photons passing through the object are ever 217 218 detected with a position-sensitive camera, is remarkable. A key 219 observation is the previously mentioned impracticality of two-step 220 GT achieved by simply combining 2D GI at each projection, with 221 standard tomographic reconstruction concepts. Rather, we em-222 phasize that direct GT was seen to be much more effective as iterative refinement occurs in a whole-of-data set manner. We 223 thereby reconstructed a 140 × 140 × 72 voxel ghost tomogram us-224 225 ing approximately 26,000 bucket measurements spread over 14 226 sample-rotation orientations, equating to over 50 reconstructed 227 voxels per bucket measurement. This efficiency was enabled by 228 harnessing *a posteriori* assumptions (or enforcing *priors*). GT is 229 particularly suited to such efficiencies, the further exploitation of which may aid in a long-term aim of reduced dose relative 230 to conventional imaging. 231

The x-ray dose in conventional CT is the product of flux-per-232 view-angle, and the number of viewing angles used. Dose reduc-233 234 tion in conventional CT is necessarily achieved by some combi-235 nation of: (i) reducing flux per viewing angle, decreasing 236 tomogram signal-to-noise ratio; or (ii) reducing the number of 237 viewing angles, typically resulting in artifacts in the tomogram 238 since the reduced sampling conditions do not satisfy the incoherence requirements of compressed sensing. 239

An effective combination of compressed sensing and CT, 240 241 known as compressive tomography (see e.g., [21-23]), uses illumi-242 nation masks to obstruct patterns of pixels from the illuminating radiation. This method has the potential to reduce dose without 243 introducing artifacts into the tomogram, as the illumination 244 masks can be constructed to satisfy the incoherence requirements 245 246 of compressed sensing. Compressive tomography can be achieved as a special case of GT, by using a pinhole mask translated to each 247 unblocked pixel element per view-angle; thus, GT can be at least 248 as effective at dose reduction, with the potential to be more so. 249

250 From a broader perspective, our demonstration of GT shows 251 how the GI approach is naturally able to relax the constraints 252 placed on image quality by dose rate, as well as on image resolution by detector performance. This is a fundamental departure 253 from conventional imaging paradigms. GT affords the flexibility 254 of independently varying a number of parameters, such as the 255 illumination masks, exposure time, number of bucket readings, 256 257 and number of object orientation angles. As a consequence, the resolution level can be optimized against dose rate in a manner 258 that takes into account prior knowledge about the sample. 259 For instance, illumination masks can be designed in a way to 260

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minimize dose to the sample (according to prior knowledge of it) while maintaining high resolution. This is not possible in direct imaging using a pixel array detector, which requires all pixels to be illuminated regardless of the object being imaged. Therefore, while it is important to compare the performance of ghost and conventional imaging-as done in this paper-it is crucial to recognize that GI is not just a different way of making images. Also, a GI or tomography system can be designed to be adaptive, in the sense that it can be optimized for the features of the object being imaged [24]. This may have great practical advantages when using ionizing radiation. For instance, it is not too far-fetched to imagine how GT with mask engineering could be used in future radiological practice. By using the available prior information, the dose could be spatially and angularly distributed to statistically match the object of interest (for instance the brain or the lungs) given that the size, shape, and density of these organs or body parts are well known.

We close this discussion with some speculations regarding pos-278 sible future challenges and limitations of GT, the overcoming of 279 which will progress the maturation of the technique. Limitations 280 are not strictly technological *per se*; many can be overcome by 281 further technique development. Significant work in GI remains 282 to realize a genuine competitive advantage with regards to dose 283 and photon budgets, relative to more conventional forms of im-284 aging, or the discovery of at least one niche area in which the 285 analyses GI provides are clearly superior. We expect a reasonably 286 straightforward translation of GT to low-flux cone-beam labora-287 tory x-ray sources through the use of computational GI, e.g., as 288 performed in Zhang et al. [8]. A challenge with a true single-pixel 289 bucket detector setup (as opposed to the accumulated bucket sig-290 nal used here) will be that of alignment. One possibility is an 291 alignment phantom and protocol that uses only signal intensity, 292 i.e., maximum intensity equates to an aligned system; a second 293 option would be an auxiliary alignment system. When consider-294 ing a computational x-ray GI setup, the question arises: What 295 magnifications could be reasonably achieved for tomographic 296 ghost microscopy? In this case the mask used to structure the il-297 lumination can be preimaged with high resolution, e.g., with a 298 transmission electron microscope. Assuming the mask has fea-299 tures up to the resolution of this prerecorded image, the limit 300 to GI and GT resolution would be that of the translation accuracy 301 of the mask, as well as the alignment with the assumed position of 302 the single-pixel detector. We anticipate that hybrid systems, com-303 bining GI with conventional imaging approaches using a 2D po-304 sition sensitive bucket detector, will be of future interest when 305 considering optimization of dose and resolution. In addition to 306 compressed sensing (e.g., [12,18]) and regularization in general 307 (as exemplified here), we expect that artificial intelligence and 308 deep learning are likely to play an important role in the future 309 evolution of whole-of-data set reconstruction approaches for 310 GT (as demonstrated by Shimobaba et al. [25] for GI). 311

#### 5. CONCLUSION

We report the experimental demonstration of GT, obtained using313hard x rays. We demonstrate that GT is able to computationally314measure the 3D internal distribution of a sample by a set of315bucket readings of the total transmitted x-ray intensity from316the sample. The task is accomplished by illuminating the sample317with a known, varying set of 2D x-ray patterns for each rotation318angle of the sample. We discussed our strategies for data319

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320 acquisition and processing, showing how direct tomographic reconstruction from bucket readings is much more effective than 321 322 the two-step approach of tomographic inversion following GI reconstruction of individual projections. These results outline 323 how the flexibility of engineering a GT measurement marks a 324 radical departure from the conventional tomographic imaging 325 paradigm, being able to make optimal use of the available 326 327 information to maximize tomogram quality and minimize the 328 radiation dose used.

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340 See Supplement 1 for supporting content.

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- 1. AU: In the sentence beginning "The relevant (spck/bckt) resolution result," do you think it might be appropriate to spell out "spck" and "bckt" for the convenience of the reader?
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1. Supplement 1 supplementary manuscript https://doi.org/10.6084/m9.figshare.7178900

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